Information about images from the size of fibers

Abstract If $X$ is a given topological space and $f: X \to Y$ is a continuous function, there are cases when information about the cardinality of the fibers $f^{-1}(y)$ gives information about the space $Y$. We discuss some old and some new results about such situations.