

**Math 101 Supplement #2**  
**Direct and Joint Variation**

Name \_\_\_\_\_  
Due \_\_\_\_\_

Part I. Find the constant of proportionality,  $k$ , then solve for the indicated value.

1.  $y$  varies directly as  $x$ .  $y = 65$  when  $x = 5$ . Find  $y$  when  $x = 12$ .
2.  $y$  varies directly as  $x$ .  $y = 45$  when  $x = 5$ . Find  $y$  when  $x = 13$ .
3.  $y$  varies jointly as  $x$  and  $z$ .  $y = 25$  when  $x = 2$  and  $z = 5$ . Find  $y$  when  $x = 8$  and  $z = 12$ .
4.  $C$  varies jointly as  $A$  and  $T$ .  $C = 175$  when  $A = 2100$  and  $T = 4$ . Find  $C$  when  $A = 2400$  and  $T = 6$ .

Part II. Write an equation that expresses each relationship. Then solve the equation for  $y$ .

5.  $x$  varies jointly as  $y$  and the square of  $z$ .
6.  $x$  varies jointly as  $z$  and the difference of  $y$  and  $w$ .

Part III. Use a variation equation to find the constant of variation (proportionality),  $k$ . Then use  $k$  to solve the problem.

7. An alligator's tail length,  $T$  varies directly as its body length,  $B$ . An alligator with a body length of 4 feet has a tail length of 3.6 feet. What is the tail length of an alligator whose body length is 6 feet.
8. On a dry asphalt road, a car's stopping distance varies directly as the square of its speed. A car traveling at 45 miles per hour can stop in 67.5 feet. What is the stopping distance for a car traveling at 60 miles per hour?

9. The heat loss of a glass window varies jointly as the window's area and the difference between the outside and inside temperatures. A window 3 feet wide by 6 feet long loses 1200 Btu per hour when the temperature outside is 20 degrees colder than the temperature inside. Find the heat loss through a glass window that is 6 feet wide by 9 feet long when the temperature outside is 10 degrees colder than the temperature inside.
  
10. Kinetic energy varies jointly as the mass and the square of the velocity. A mass of 8 grams and velocity of 3 centimeters per second has a kinetic energy of 36 ergs. Find the kinetic energy for a mass of 4 grams and velocity of 6 centimeters per second.
  
11. The volume of a pyramid varies jointly as its height and the area of its base. A pyramid with a height of 15 feet and a base with an area of 35 square feet has a volume of 175 cubic feet. Find the height of a pyramid which has a volume of 800 cubic feet and base area of 120 square feet.